

Package: metaquant (via r-universe)

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Title Meta-Analysis of Quantiles and Functions of Quantiles

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Description Implements a novel density-based approach for estimating unknown parameters, distribution visualisations and meta-analyses of quantiles and their functions. A detailed vignettes with example datasets and code to prepare data and analyses is available at <https://bookdown.org/a2delivera/metaquant/>. The methods are described in the pre-print by De Livera, Prendergast and Kumaranathunga (2024, <doi:10.48550/arXiv.2411.10971>).

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est.gld.five	<i>Estimating Unknown Parameters using Five-Number Summary</i>
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Description

This function provide estimates for the parameters of generalised lambda distribution (GLD), the sample mean and the standard deviation using 5-number summary { minimum, first quartile, median, third quartile, maximum } from a study with sample size n , using the method explained in De Livera et al. (2024).

Usage

```
est.gld.five(
  min = NULL,
  q1 = NULL,
  med = NULL,
  q3 = NULL,
  max = NULL,
  n = NULL,
  opt = TRUE
)
```

Arguments

min	numeric value representing the sample minimum.
q1	numeric value representing the first quartile of the sample.
med	numeric value representing the median of the sample.
q3	numeric value representing the third quartile of the sample.
max	numeric value representing the sample maximum.
n	numeric value specifying the sample size.
opt	logical value indicating whether to apply the optimisation step in estimating parameters using theoretical quantiles. The default value is TRUE.

Details

De Livera et al. (2024) proposed using the generalised lambda distribution (GLD) to estimate unknown parameters for studies reporting 5-number summaries in the meta-analysis context.

The GLD is a four parameter family of distributions defined by its quantile function under the FKML parameterisation (Freimer et al., 1988). De Livera et al. propose that the GLD quantile function can be used to approximate a sample's distribution using 5-point summaries. The four parameters of GLD quantile function include: a location parameter (λ_1), an inverse scale parameter ($\lambda_2 > 0$), and two shape parameters (λ_3 and λ_4). The parameters of the GLD are estimated by formulating and solving a set of simultaneous equations which relate the estimated sample quantiles to their theoretical counterparts of the GLD.

Value

A list with following components:

- parameters: named numeric vector representing the estimated parameters ('location', 'inverse scale', 'shape 1', 'shape 2') of GLD .
- mean: numeric value of the estimated mean of the sample using GLD.
- sd: numeric value of the estimated standard deviation of the sample using GLD.

References

De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.

Freimer, M., Kollia, G., Mudholkar, G. S., & Lin, C. T. (1988). A study of the generalized Tukey lambda family. *Communications in Statistics—Theory and Methods*, 17(10), 3547–3567.

Gilchrist, W. (2000). *Statistical modelling with quantile functions*. Chapman & Hall/CRC.

King, R., Dean, B., Klinke, S., & van Staden, P. (2025). gld: Estimation and use of the Generalised (Tukey) Lambda Distribution (R package Version 2.6.7). Comprehensive R Archive Network (CRAN). <https://doi.org/10.32614/CRAN.package.gld>. <https://CRAN.R-project.org/package=gld>.

See Also

[est.sld.minq2max\(\)](#), [est.sld.q1q2q3\(\)](#)

Examples

```
#Generate 5-number summary data
set.seed(123)
n <- 1000
x <- stats::rlnorm(n, 4, 0.3)
quants <- c(min(x), stats::quantile(x, probs = c(0.25, 0.5, 0.75)), max(x))

#Estimate GLD parameters using 5-number summary
params<- est.gld.five(min = quants[1], q1 = quants[2], med = quants[3], q3 = quants[4],
                    max = quants[5], n=n, opt=TRUE)$parameters
```

params

est.mean

Estimating Sample Mean using Quantiles

Description

This function estimates the sample mean from a study presenting quantile summary measures with the sample size (n). The quantile summaries can fall into one of the following categories:

- S_1 : { minimum, median, maximum }
- S_2 : { first quartile, median, third quartile }
- S_3 : { minimum, first quartile, median, third quartile, maximum }

The `est.mean` function implements newly proposed flexible quantile-based distribution methods for estimating sample mean (De Livera et al., 2024). It also incorporates existing methods for estimating sample means as described by Luo et al. (2018) and McGrath et al. (2020).

Usage

```
est.mean(
  min = NULL,
  q1 = NULL,
  med = NULL,
  q3 = NULL,
  max = NULL,
  n = NULL,
  method = "gld/sld",
  opt = TRUE
)
```

Arguments

<code>min</code>	numeric value representing the sample minimum.
<code>q1</code>	numeric value representing the first quartile of the sample.
<code>med</code>	numeric value representing the median of the sample.
<code>q3</code>	numeric value representing the third quartile of the sample.
<code>max</code>	numeric value representing the sample maximum.
<code>n</code>	numeric value specifying the sample size.
<code>method</code>	character string specifying the approach used to estimate the sample means. The options are the following: ' <code>gld/sld</code> ' The default option. The method proposed by De Livera et al. (2024). Estimation using the generalised lambda distribution (GLD) for 5-number summaries (S_3), and the skew logistic distribution (SLD) for 3-number summaries (S_1 and S_2).

	'luo' Method of Luo et al. (2018).
	'hozo/wan/bland' The method proposed by Wan et al. (2014). i.e., the method of Hozo et al. (2005) for S_1 , method of Wan et al. (2014) for S_2 , and method of Bland (2015) for S_3 .
	'bc' Box-Cox method proposed by McGrath et al. (2020).
	'qe' Quantile Matching Estimation method proposed by McGrath et al. (2020).
opt	logical value indicating whether to apply the optimisation step of 'gld/sld' method, in estimating their parameters using theoretical quantiles. The default value is TRUE.

Details

The 'gld/sld' method (i.e., the method of De Livera et al., (2024)) of `est.mean` uses the following quantile based distributions:

- Generalised Lambda Distribution (GLD) for estimating the sample mean using 5-number summaries (S_3).
- Skew Logistic Distribution (SLD) for estimating the sample mean using 3-number summaries (S_1 and S_2).

The generalised lambda distribution (GLD) is a four parameter family of distributions defined by its quantile function under the FKML parameterisation (Freimer et al., 1988). De Livera et al. propose that the GLD quantile function can be used to approximate a sample's distribution using 5-point summaries. The four parameters of GLD quantile function include: a location parameter (λ_1), an inverse scale parameter ($\lambda_2 > 0$), and two shape parameters (λ_3 and λ_4).

The quantile-based skew logistic distribution (SLD), introduced by Gilchrist (2000) and further modified by van Staden and King (2015) is used to approximate the sample's distribution using 3-point summaries. The SLD quantile function is defined using three parameters: a location parameter (λ), a scale parameter (η), and a skewing parameter (δ).

For 'gld/sld' method, the parameters of the GLD and SLD are estimated by formulating and solving a set of simultaneous equations. These equations relate the estimated sample quantiles to their theoretical counterparts of the respective distribution (GLD or SLD). Finally, the mean for each scenario is calculated by integrating functions of the estimated quantile function.

Value

mean: numeric value representing the estimated mean of the sample.

References

- De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.
- Luo, D., Wan, X., Liu, J., & Tong, T. (2018). Optimally estimating the sample mean from the sample size, median, mid-range, and/or mid-quartile range. *Statistical methods in medical research*, 27(6), 1785-1805.

Description

This function estimates the variances of quantiles and the differences of quantiles for single-group and two-group studies, respectively, from studies that report five-number summaries (minimum, first quartile, median, third quartile, maximum) and sample sizes, using density-based approaches.

The `est.q.study.level` function currently supports two density-based frameworks: (1) a Generalized Lambda Distribution (GLD) fitted via percentile matching, following De Livera et al. (2024); and (2) an extension of the Quantile Estimation (QE) method of McGrath et al. (2020) to additional quantiles and functions of quantiles.

The function estimates the asymptotic variances of the following effect sizes:

- Single-group quantiles: median (m), first quartile (q_1), third quartile (q_3).
- Two-group differences in quantiles: difference in medians ($m_{g1} - m_{g2}$), difference in first quartiles ($q_{1g1} - q_{1g2}$), difference in third quartiles ($q_{3g1} - q_{3g2}$).

Portions of this implementation are adapted from [qe.study.level](#) for the QE method, and have been extended to support other quantiles and functions of quantiles beyond the median.

Usage

```
est.q.study.level(  
  min.g1,  
  q1.g1,  
  med.g1,  
  q3.g1,  
  max.g1,  
  n.g1,  
  min.g2,  
  q1.g2,  
  med.g2,  
  q3.g2,  
  max.g2,  
  n.g2,  
  method,  
  effect.size.type,  
  opt = TRUE,  
  single.family = FALSE,  
  qe.fit.control.g1 = list(),  
  qe.fit.control.g2 = list()  
)
```

Arguments

<code>min.g1</code>	numeric value representing the sample minimum (of group one for two-group studies).
<code>q1.g1</code>	numeric value representing the first quartile of the sample (of group one for two-group studies).
<code>med.g1</code>	numeric value representing the median of the sample (of group one for two-group studies).
<code>q3.g1</code>	numeric value representing the third quartile of the sample (of group one for two-group studies).
<code>max.g1</code>	numeric value representing the sample maximum (of group one for two-group studies).
<code>n.g1</code>	numeric value specifying the sample size (of group one for two-group studies).
<code>min.g2</code>	numeric value representing the sample minimum of group two for two-group studies.
<code>q1.g2</code>	numeric value representing the first quartile of the sample of group two for two-group studies.
<code>med.g2</code>	numeric value representing the median of the sample of group two for two-group studies.
<code>q3.g2</code>	numeric value representing the third quartile of the sample of group two for two-group studies.
<code>max.g2</code>	numeric value representing the sample maximum of group two for two-group studies.
<code>n.g2</code>	numeric value specifying the sample size of group two for two-group studies.
<code>method</code>	character string specifying the density-based approach used to estimate variances of quantiles or their functions. Options: <ul style="list-style-type: none"> 'gld' The default option. Estimation method proposed by De Livera et al. (2024) using the generalised lambda distribution (GLD). 'qe' Quantile Matching Estimation method proposed by McGrath et al. (2020).
<code>effect.size.type</code>	character string specifying the quantile-based effect size for the meta-analysis. Options: <ul style="list-style-type: none"> 'median' The default option. Median for single-group studies; difference in medians for two-group studies. 'q1' First quartile for single-group studies; difference in first quartiles for two-group studies. 'q3' Third quartile for single-group studies; difference in third quartiles for two-group studies.
<code>opt</code>	logical; whether to apply the optimisation step of the "gld" method when estimating its parameters. Default is TRUE.
<code>single.family</code>	logical; for two-group studies using the "qe" method, whether to assume the same parametric family of distributions for both groups. Default is FALSE. See qe.study.level

- qe.fit.control.g1
optional list of control parameters for `qe.fit` (of group one for two-group studies).
- qe.fit.control.g2
optional list of control parameters for `qe.fit` of group two for two-group studies.

Value

A list containing following components:

- `effect.size`: numeric value of quantile-based effect size of the study based on the input of `effect.size.type` argument.
- `estvar`: numeric value of the estimated variance of the effect size.
- `number.of.groups`: integer indicating the number of groups in the input study data.
- `effect.size.name`: character string specifying a label for the effect size depending on `number.of.groups` and `effect.size.type`.

References

De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.

King, R., Dean, B., Klinke, S., & van Staden, P. (2025). `gld`: Estimation and use of the Generalised (Tukey) Lambda Distribution (R package Version 2.6.7). Comprehensive R Archive Network (CRAN). <https://doi.org/10.32614/CRAN.package.gld>. <https://CRAN.R-project.org/package=gld>.

McGrath, S., Sohn, H., Steele, R., & Benedetti, A. (2020). Meta-analysis of the difference of medians. *Biometrical Journal*, 62(1), 69-98.

McGrath, S., Zhao, X., Ozturk, O., Katzenschlager, S., Steele, R., & Benedetti, A. (2024). Meta-median: an R package for meta-analyzing studies reporting medians. *Research Synthesis Methods*, 15(2), 332-346.

See Also

[est.r.study.level\(\)](#)

Examples

```
#Generate 5-number summary data (group one)
set.seed(123)
n1 <- 100
x1 <- stats::rlnorm(n1, 4, 0.3)
quants1 <- c(min(x1), stats::quantile(x1, probs = c(0.25, 0.5, 0.75)), max(x1))

#Estimate variance of the first quartile
est.q.study.level(min.g1 = quants1[1], q1.g1 = quants1[2], med.g1 = quants1[3],
                 q3.g1 = quants1[4], max.g1 = quants1[5], n.g1=n1,
                 method = "gld", effect.size.type = "q1")
```

```

#Generate 5-number summary data (group two)
set.seed(123)
n2 <- 120
x2 <- stats::rlnorm(n2, 3, 0.5)
quants2 <- c(min(x2), stats::quantile(x2, probs = c(0.25, 0.5, 0.75)), max(x2))

#Estimate variance of the difference in first quartiles (for two groups)
est.q.study.level(min.g1 = quants1[1], q1.g1 = quants1[2], med.g1 = quants1[3],
  q3.g1 = quants1[4], max.g1 = quants1[5], n.g1=n1,
  min.g2 = quants2[1], q1.g2 = quants2[2], med.g2 = quants2[3],
  q3.g2 = quants2[4], max.g2 = quants2[5], n.g2=n2,
  method = "gld", effect.size.type = "q1")

```

est.r.study.level *Estimating Variances of Squared IQR Ratio and its Natural Logarithm*

Description

This function estimates the variances of squared IQR ratio and its logarithm for two-group studies, from studies that report five-number summaries (minimum, first quartile, median, third quartile, maximum) and sample sizes, using density-based approaches.

The `est.r.study.level` function currently supports two density-based frameworks: (1) a Generalized Lambda Distribution (GLD) fitted via percentile matching, following De Livera et al. (2024); and (2) an extension of the Quantile Estimation (QE) method of McGrath et al. (2020) to additional quantiles and functions of quantiles.

The function estimates the asymptotic variances of the following effect sizes:

- Ratio of squared interquartile ranges (IQRs) between two groups: $r = (q_{3g1} - q_{1g1})^2 / (q_{3g2} - q_{1g2})^2$.
- Log ratio of squared IQRs between two groups: $\log(r)$.

Portions of this implementation are adapted from [qe.study.level](#) for the QE method, and have been extended to support functions of quantiles beyond the median.

Usage

```

est.r.study.level(
  min.g1,
  q1.g1,
  med.g1,
  q3.g1,
  max.g1,
  n.g1,
  min.g2,
  q1.g2,

```

```

    med.g2,
    q3.g2,
    max.g2,
    n.g2,
    method,
    opt = TRUE,
    single.family = FALSE,
    qe.fit.control.g1 = list(),
    qe.fit.control.g2 = list()
)

```

Arguments

min.g1	numeric value representing the sample minimum (of group one for two-group studies).
q1.g1	numeric value representing the first quartile of the sample (of group one for two-group studies).
med.g1	numeric value representing the median of the sample (of group one for two-group studies).
q3.g1	numeric value representing the third quartile of the sample (of group one for two-group studies).
max.g1	numeric value representing the sample maximum (of group one for two-group studies).
n.g1	numeric value specifying the sample size (of group one for two-group studies).
min.g2	numeric value representing the sample minimum of group two for two-group studies.
q1.g2	numeric value representing the first quartile of the sample of group two for two-group studies.
med.g2	numeric value representing the median of the sample of group two for two-group studies.
q3.g2	numeric value representing the third quartile of the sample of group two for two-group studies.
max.g2	numeric value representing the sample maximum of group two for two-group studies.
n.g2	numeric value specifying the sample size of group two for two-group studies.
method	character string specifying the density-based approach used to estimate variances of squared IQR ratio and its natural logarithm. Options: 'gld' The default option. Estimation method proposed by De Livera et al. (2024) using the generalised lambda distribution (GLD). 'qe' Quantile Matching Estimation method proposed by McGrath et al. (2020).
opt	logical; whether to apply the optimisation step of the "gld" method when estimating its parameters. Default is TRUE.
single.family	logical; for two-group studies using the "qe" method, whether to assume the same parametric family of distributions for both groups. Default is FALSE. See qe.study.level

- `qe.fit.control.g1`
optional list of control parameters for `qe.fit` (of group one for two-group studies).
- `qe.fit.control.g2`
optional list of control parameters for `qe.fit` of group two for two-group studies.

Value

A list containing following components:

- `effect.size`: numeric value of the effect size of the study (ratio of squared IQRs).
- `estvar`: estimated variance of the effect size (ratio of squared IQRs).
- `effect.size.log`: numeric value of log ratio of squared IQRs.
- `estvar.log`: estimated variance of log ratio of squared IQRs.
- `number.of.groups`: integer indicating the number of groups in the input study data.

References

De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.

King, R., Dean, B., Klinke, S., & van Staden, P. (2025). `gld`: Estimation and use of the Generalised (Tukey) Lambda Distribution (R package Version 2.6.7). Comprehensive R Archive Network (CRAN). <https://doi.org/10.32614/CRAN.package.gld>. <https://CRAN.R-project.org/package=gld>.

McGrath, S., Sohn, H., Steele, R., & Benedetti, A. (2020). Meta-analysis of the difference of medians. *Biometrical Journal*, 62(1), 69-98.

McGrath, S., Zhao, X., Ozturk, O., Katzenschlager, S., Steele, R., & Benedetti, A. (2024). Meta-median: an R package for meta-analyzing studies reporting medians. *Research Synthesis Methods*, 15(2), 332-346.

See Also

[est.q.study.level\(\)](#)

Examples

```
#Generate 5-number summary data (group one)
set.seed(123)
n1 <- 100
x1 <- stats::rlnorm(n1, 4, 0.3)
quants1 <- c(min(x1), stats::quantile(x1, probs = c(0.25, 0.5, 0.75)), max(x1))

#Generate 5-number summary data (group two)
set.seed(123)
n2 <- 120
x2 <- stats::rlnorm(n2, 3, 0.5)
```

```

quants2 <- c(min(x2), stats::quantile(x2, probs = c(0.25, 0.5, 0.75)), max(x2))

#Estimate variance of the squared IQR ratio and its natural logarithm (for two groups)
est.r.study.level(min.g1 = quants1[1], q1.g1 = quants1[2], med.g1 = quants1[3],
                  q3.g1 = quants1[4], max.g1 = quants1[5], n.g1=n1,
                  min.g2 = quants2[1], q1.g2 = quants2[2], med.g2 = quants2[3],
                  q3.g2 = quants2[4], max.g2 = quants2[5], n.g2=n2,
                  method = "gld")

```

est.sd

Estimating Sample Standard Deviation using Quantiles

Description

This function estimates the sample standard deviation from a study presenting quantile summary measures with the sample size (n). The quantile summaries can fall into one of the following categories:

- S_1 : { minimum, median, maximum }
- S_2 : { first quartile, median, third quartile }
- S_3 : { minimum, first quartile, median, third quartile, maximum }

The `est.sd` function implements newly proposed flexible quantile-based distribution methods for estimating sample standard deviation by De Livera et al. (2024) as well as other existing methods for estimating sample standard deviations by Shi et al. (2020) and McGrath et al. (2020).

Usage

```

est.sd(
  min = NULL,
  q1 = NULL,
  med = NULL,
  q3 = NULL,
  max = NULL,
  n = NULL,
  method = "shi/wan",
  opt = TRUE
)

```

Arguments

<code>min</code>	numeric value representing the sample minimum.
<code>q1</code>	numeric value representing the first quartile of the sample.
<code>med</code>	numeric value representing the median of the sample.
<code>q3</code>	numeric value representing the third quartile of the sample.

max	numeric value representing the sample maximum.
n	numeric value specifying the sample size.
method	character string specifying the approach used to estimate the sample standard deviations. The options are the following: 'shi/wan' The default option. Method of Shi et al. (2020). 'gld/sld' The method proposed by De Livera et al. (2024). Estimation using the generalised lambda distribution (GLD) for 5-number summaries (S_3), and the skew logistic distribution (SLD) for 3-number summaries (S_1 and S_2). 'wan' The method proposed by Wan et al. (2014). 'bc' Box-Cox method proposed by McGrath et al. (2020). 'qe' Quantile Matching Estimation method proposed by McGrath et al. (2020).
opt	logical value indicating whether to apply the optimisation step of 'gld/sld' method, in estimating their parameters using theoretical quantiles. The default value is TRUE.

Details

For details explaining the new method 'gld/sld', check [est.mean](#).

Value

sd: numeric value representing the estimated standard deviation of the sample.

References

- De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.
- Shi, J., Luo, D., Weng, H., Zeng, X.-T., Lin, L., Chu, H., & Tong, T. (2020). Optimally estimating the sample standard deviation from the five-number summary. *Research Synthesis Methods*, *11*(5), 641–654.
- Wan, X., Wang, W., Liu, J., & Tong, T. (2014). Estimating the sample mean and standard deviation from the sample size, median, range and/or interquartile range. *BMC Medical Research Methodology*, *14*, 1–13.
- McGrath, S., Zhao, X., Steele, R., Thombs, B. D., Benedetti, A., & the DEPRESSD Collaboration. (2020b). Estimating the sample mean and standard deviation from commonly reported quantiles in meta-analysis. *Statistical Methods in Medical Research*, *29*(9), 2520–2537.

Examples

```
#Generate 5-point summary data
set.seed(123)
n <- 1000
x <- stats::rlnorm(n, 5, 0.5)
quants <- c(min(x), stats::quantile(x, probs = c(0.25, 0.5, 0.75)), max(x))
obs_sd <- sd(x)
```

```

#Estimate sample SD using s3 (5 number summary)
est_sd_s3 <- est.sd(min = quants[1], q1 = quants[2], med = quants[3], q3 = quants[4],
                  max = quants[5], n=n, method = "gld/sld")
est_sd_s3

#Estimate sample SD using s1 (min, median, max)
est_sd_s1 <- est.sd(min = quants[1], med = quants[3], max = quants[5],
                  n=n, method = "gld/sld")
est_sd_s1

#Estimate sample SD using s2 (q1, median, q3)
est_sd_s2 <- est.sd(q1 = quants[2], med = quants[3], q3 = quants[4],
                  n=n, method = "gld/sld")
est_sd_s2

```

est.sld.minq2max	<i>Estimating Unknown Parameters using Minimum, Median and Maximum</i>
------------------	--

Description

This function provide estimates for the parameters of skew logistic distribution (SLD), the sample mean and the standard deviation using 3-number summary {minimum, median (q_2), maximum} from a study with sample size n , using the method explained in De Livera et al. (2024).

Usage

```

est.sld.minq2max(
  min = NULL,
  med = NULL,
  max = NULL,
  n = NULL,
  opt = TRUE
)

```

Arguments

min	numeric value representing the sample minimum.
med	numeric value representing the median of the sample.
max	numeric value representing the sample maximum.
n	numeric value specifying the sample size.
opt	logical value indicating whether to apply the optimisation step in estimating parameters using theoretical quantiles. The default value is TRUE.

est.sld.q1q2q3

*Estimating Unknown Parameters using First Quartile, Median and Third Quartile***Description**

This function provide estimates for the parameters of skew logistic distribution (SLD), the sample mean and the standard deviation using 3-number summary {first quartile (q_1), median (q_2), third quartile (q_3)} from a study with sample size n , using the method explained in De Livera et al. (2024).

Usage

```
est.sld.q1q2q3(
  q1 = NULL,
  med = NULL,
  q3 = NULL,
  n = NULL,
  opt = TRUE
)
```

Arguments

q1	numeric value representing the first quartile of the sample.
med	numeric value representing the median of the sample.
q3	numeric value representing the third quartile of the sample.
n	numeric value specifying the sample size.
opt	logical value indicating whether to apply the optimisation step in estimating parameters using theoretical quantiles. The default value is TRUE.

Details

De Livera et al. (2024) proposed using the skew logistic distribution (SLD) to estimate unknown parameters for studies reporting 3-number summaries in the meta-analysis context.

The quantile-based skew logistic distribution, introduced by Gilchrist (2000) and further modified by van Staden and King (2015) is used to approximate the sample's distribution using 3-point summaries. The SLD quantile function is defined using three parameters: a location parameter (λ), a scale parameter (η), and a skewing parameter (δ). The parameters of the SLD are estimated by formulating and solving a set of simultaneous equations which relate the estimated sample quantiles to their theoretical counterparts of the SLD.

Value

A list with following components:

- parameters: named numeric vector representing the estimated parameters ('location', 'scale', 'skewing') of SLD.

- mean: numeric value of the estimated mean of the sample using SLD.
- sd: numeric value of the estimated standard deviation of the sample using SLD.

References

De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.

Gilchrist, W. (2000). *Statistical modelling with quantile functions*. Chapman & Hall/CRC.

van Staden, P. J., & King, R. A. R. (2015). The quantile-based skew logistic distribution. *Statistics & Probability Letters*, *96*, 109–116.

King, R., & van Staden, P. (2022). sld: Estimation and use of the Quantile-Based Skew Logistic Distribution (R package Version 1.0.1). Comprehensive R Archive Network (CRAN). <https://doi.org/10.32614/CRAN.package.sld>. [#https://CRAN.R-project.org/package=sld.#](https://CRAN.R-project.org/package=sld)

See Also

[est.gld.five\(\)](#), [est.sld.minq2max\(\)](#)

Examples

```
#Generate 3-number summary data
set.seed(123)
n <- 1000
x <- stats::rlnorm(n, 4, 0.3)
quants <- c(stats::quantile(x, probs = c(0.25, 0.5, 0.75)))

#Estimate SLD parameters using 3-number summary
params<- est.sld.q1q2q3(q1 = quants[1], med = quants[2], q3 = quants[3],
                      n=n, opt=TRUE)$parameters

params
```

metaquant

Meta-Analysis of Quantiles and Functions of Quantiles

Description

This function implements statistical methods for meta-analysis of quantiles and functions of quantiles for single-group and two-group studies. The function uses inverse-variance weighting to synthesise information from studies that report five-number summaries (minimum, first quartile, median, third quartile, maximum) and sample sizes—particularly useful for skewed outcomes.

The metaquant function currently supports two density-based frameworks: (1) a Generalized Lambda Distribution (GLD) fitted via percentile matching, following De Livera et al. (2024), to estimate parameters for meta-analysis of medians and other quantiles; and (2) an extension of the Quantile Estimation (QE) method of McGrath et al. (2020) to additional quantiles and functions of quantiles, with derived standard errors for inverse-variance pooling.

The function facilitates meta-analyses of the following effect sizes:

- Single-group quantiles: median (m), first quartile (q_1), third quartile (q_3).
- Two-group differences in quantiles: difference in medians ($m_{g1} - m_{g2}$), difference in first quartiles ($q_{1g1} - q_{1g2}$), difference in third quartiles ($q_{3g1} - q_{3g2}$).
- Ratio of squared interquartile ranges (IQRs) between two groups: $r = (q_{3g1} - q_{1g1})^2 / (q_{3g2} - q_{1g2})^2$.

Portions of this implementation are adapted from [metamedian](#) for the QE method, and have been extended to support other quantiles and functions of quantiles beyond the median.

Usage

```
metaquant(
  data,
  method = "gld",
  effect.size.type = "median",
  opt = TRUE,
  single.family = FALSE,
  pool.studies = TRUE,
  ...)
```

Arguments

data a data frame with one row per study containing five-number summaries and sample sizes. For one-group studies, the input should contain the following columns:

- 'min.g1' minimum value
- 'q1.g1' first quartile
- 'med.g1' median
- 'q3.g1' third quartile
- 'max.g1' maximum value
- 'n.g1' sample size

For two-group studies, also include the corresponding columns for the second group: min.g2, q1.g2, med.g2, q3.g2, max.g2, and n.g2.

method character string specifying the density-based approach used to perform the meta analysis of quantiles or their functions. Options:

- 'gld' The default option. Estimation method proposed by De Livera et al. (2024) using the generalised lambda distribution (GLD).
- 'qe' Quantile Matching Estimation method proposed by McGrath et al. (2020).

effect.size.type character string specifying the quantile-based effect size for the meta-analysis. Options:

- 'median' The default option. Median for single-group studies; difference in medians for two-group studies.
- 'q1' First quartile for single-group studies; difference in first quartiles for two-group studies.

	'q3'	Third quartile for single-group studies; difference in third quartiles for two-group studies.
	'logr2'	Log ratio of squared IQRs between two groups. Only applicable when the input data frame provides columns for both groups.
opt		logical; whether to apply the optimisation step of the "gld" method when estimating its parameters. Default is TRUE.
single.family		logical; for two-group studies using the "qe" method, whether to assume the same parametric family of distributions for both groups. Default is FALSE. See qe.study.level .
pool.studies		logical; whether to pool study-specific effect sizes via inverse-variance-weighted meta-analysis. Default is TRUE. If FALSE, the function returns a list of effect sizes and their within-study variance estimates. See rma.uni .
...		additional arguments passed to rma.uni for pooling.

Value

An object of class "rma.uni" or a list of effect sizes and their estimated variances.

References

- De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.
- King, R., Dean, B., Klinke, S., & van Staden, P. (2025). gld: Estimation and use of the Generalised (Tukey) Lambda Distribution (R package Version 2.6.7). Comprehensive R Archive Network (CRAN). <https://doi.org/10.32614/CRAN.package.gld>. <https://CRAN.R-project.org/package=gld>.
- McGrath, S., Sohn, H., Steele, R., & Benedetti, A. (2020). Meta-analysis of the difference of medians. *Biometrical Journal*, 62(1), 69-98.
- McGrath, S., Zhao, X., Ozturk, O., Katzenschlager, S., Steele, R., & Benedetti, A. (2024). Meta-median: an R package for meta-analyzing studies reporting medians. *Research Synthesis Methods*, 15(2), 332-346.

See Also

[est.mean\(\)](#), [est.sd\(\)](#)

Examples

```
# Example dataset of 5-number summaries (min, q1, med, q3, max) for 2 groups
data_2g <- data.frame(
  study.index = c("Study1", "Study2", "Study3"),
  min.g1 = c(15, 15, 13),
  q1.g1 = c(57, 59, 55),
  med.g1 = c(66, 68, 60),
  q3.g1 = c(74, 72, 69),
  max.g1 = c(108, 101, 100),
  n.g1 = c(226, 230, 200),
```

```

min.g2 = c(18, 19, 15),
q1.g2  = c(66, 71, 69),
med.g2 = c(73, 82, 81),
q3.g2  = c(80, 93, 89),
max.g2 = c(110, 115, 100),
n.g2   = c(226, 230, 200)
)
print(data_2g)

# Meta-analysis of difference in first quartiles
metaquant(data = data_2g, method = "gld", effect.size.type = "q1")
metaquant(data = data_2g, method = "qe", effect.size.type = "q1")

# Meta-analysis of log ratio of squared IQRs
ma_lr <- metaquant(data = data_2g, method = "gld", effect.size.type = "logr2")
# Back-transform to original scale (ratio of squared IQRs)
est_r <- exp(ma_lr$b) # pooled estimate
ci_r <- exp(c(ma_lr$ci.lb, ma_lr$ci.ub)) # confidence interval
pi_r <- exp(c(predict(ma_lr)$pi.lb, predict(ma_lr)$pi.ub)) # prediction interval
est_r; ci_r; pi_r

```

Description

The function estimates and visualizes the density curves of one-group or two-group studies presenting quantile summary measures with the sample size (n). The quantile summaries can fall into one of the following categories:

- S_1 : { minimum, median, maximum }
- S_2 : { first quartile, median, third quartile }
- S_3 : { minimum, first quartile, median, third quartile, maximum }

The `plotdist` function uses the following quantile-based distribution methods for visualising densities using quantiles (De Livera et al., 2024).

- Generalised Lambda Distribution (GLD) when 5-number summaries present (S_3).
- Skew Logistic Distribution (SLD) when 3-number summaries present (S_1 and S_2).

Usage

```

plotdist(
  data,
  xmin = NULL,
  xmax = NULL,
  ymax = NULL,
  length.out = 1000,

```

```

title = "",
xlab = "x",
ylab = "Density",
line.size = 0.5,
title.size = 12,
lab.size = 10,
color.g1 = "pink",
color.g2 = "skyblue",
color.g1.pooled = "red",
color.g2.pooled = "blue",
label.g1 = NULL,
label.g2 = NULL,
display.index = FALSE,
display.legend = FALSE,
pooled.dist = FALSE,
pooled.only = FALSE,
opt = TRUE
)

```

Arguments

data	<p>data frame containing the quantile summary data. For one-group studies, the input may contain the following columns depending on the quantile scenario:</p> <ul style="list-style-type: none"> 'study.index' study index or name 'min.g1' minimum value 'q1.g1' first quartile 'med.g1' median 'q3.g1' third quartile 'max.g1' maximum value 'n.g1' sample size <p>For two-group studies, the data frame may also contain the following columns for the second group: min.g2, q1.g2, med.g2, q3.g2, max.g2 and n.g2. Note that, for three-point summaries (S_1 and S_2), only the relevant columns should be included.</p>
xmin	<p>numeric value for the lower limit of the x-axis for density calculation. It is recommended to set this to a value smaller than the smallest value across the quantile summaries to ensure the density curve is fully captured. If xmin is not provided, the minimum value of the 'min.' columns will be used for scenario S_1 or S_3. Note that for scenario S_2, no default calculation is performed for xmin.</p>
xmax	<p>numeric value for the upper limit of the x-axis for density calculation. It is recommended to set this to a value larger than the largest value across the quantile summaries to ensure the density curve is fully captured. If xmax is not provided, the maximum value of the 'max.' columns will be used for scenario S_1 or S_3. Similarly, for scenario S_2, no default calculation is performed for xmax.</p>
ymax	<p>numeric value for the upper limit of the y-axis. If NULL, the highest density value will be used.</p>

length.out	integer specifying the number of points along the x-axis for density calculation. Default is 1000.
title	character string for the plot title. Default is an empty string.
xlab	character string for the x-axis label. Default is "x".
ylab	character string for the y-axis label. Default is "Density".
line.size	numeric. Thickness of the density curve lines. Default is 0.5.
title.size	numeric. Font size for the plot title. Default is 12.
lab.size	numeric. Font size for axis labels. Default is 10.
color.g1	character string specifying the color for individual density curves of group 1 for each study (row). Default is "pink".
color.g2	character string specifying the color for individual density curves of group 2 for each study (row). Default is "skyblue".
color.g1.pooled	character string specifying the color for pooled density curve of group 1. Default is "red".
color.g2.pooled	character string specifying the color for pooled density curve of group 2. Default is "blue".
label.g1	character string indicating label or name for group 1 (eg., 'Treatment')
label.g2	character string indicating label or name for group 2 (eg., 'Control'). If 'label.g1' and 'label.g2' are not provided, the function will assign labels as 'Group 1' and 'Group 2'.
display.index	logical. If TRUE, the 'study.index' of each quantile set (row) will be displayed alongside the corresponding density curve. The default is FALSE, meaning no labels will be shown. The label text size is controlled by the lab.size parameter.
display.legend	logical. If TRUE, legends ('label.g1' and/or 'label.g2') will be displayed on the right side of the plot. The default is FALSE. The legend text size is controlled by the lab.size parameter.
pooled.dist	logical. If TRUE, pooled density curves for group 1 and/or group 2 will be plotted along with the individual density curves. The default is FALSE.
pooled.only	logical. If TRUE, only the pooled density curves of group 1 and/or group 2 will be plotted, excluding the individual density curves. The default is FALSE.
opt	logical value indicating whether to apply the optimization step when estimating GLD or SLD parameters. The default value is TRUE.

Details

The generalised lambda distribution (GLD) is a four parameter family of distributions defined by its quantile function under the FKML parameterisation (Freimer et al., 1988). De Livera et al. propose that the GLD quantile function can be used to approximate a sample's distribution using 5-point summaries. The four parameters of GLD quantile function include: a location parameter (λ_1), an inverse scale parameter ($\lambda_2 > 0$), and two shape parameters (λ_3 and λ_4).

The quantile-based skew logistic distribution (SLD), introduced by Gilchrist (2000) and further modified by van Staden and King (2015) is used to approximate the sample's distribution using 3-point summaries. The SLD quantile function is defined using three parameters: a location parameter (λ), a scale parameter (η), and a skewing parameter (δ).

These parameters of GLD and SLD are estimated by formulating and solving a series of simultaneous equations which relate the estimated quantiles with the population counterparts of respective distribution (GLD or SLD). The `plotdist` uses these estimated parameters, to compute the density data using `dgl` function from the `gld` package and `dsl` function from the `sld` package.

If one needs to generate pooled density plots, they can use the `pooled.dist` or `pooled.only` arguments as described in the *Arguments* section. The pooled density curves represent a weighted average of individual study densities, with weights determined by sample sizes. The method is similar to obtaining pooled estimates of effects in a standard meta-analysis and it serves as a way to visualize combined estimated distributional information across studies.

Value

An interactive plotly object visualizing the estimated density curve(s) for one or two groups.

References

De Livera, A. M., Prendergast, L., & Kumaranathunga, U. (2024). A novel density-based approach for estimating unknown means, distribution visualisations and meta-analyses of quantiles. *arXiv preprint arXiv:2411.10971*. <https://arxiv.org/abs/2411.10971>.

Freimer, M., Kollia, G., Mudholkar, G. S., & Lin, C. T. (1988). A study of the generalized Tukey lambda family. *Communications in Statistics—Theory and Methods*, 17(10), 3547–3567.

Gilchrist, W. (2000). *Statistical modelling with quantile functions*. Chapman & Hall/CRC.

van Staden, P. J., & King, R. A. R. (2015). The quantile-based skew logistic distribution. *Statistics & Probability Letters*, 96, 109–116.

Examples

```
#Example dataset of 3-point summaries (min, med, max) for 2 groups
data_3num_2g <- data.frame(
  study.index = c("Study 1", "Study 2", "Study 3"),
  min.g1 = c(15, 15, 13),
  med.g1 = c(66, 68, 63),
  max.g1 = c(108, 101, 100),
  n.g1 = c(226, 230, 200),
  min.g2 = c(18, 19, 15),
  med.g2 = c(73, 82, 81),
  max.g2 = c(110, 115, 100),
  n.g2 = c(226, 230, 200)
)
print(data_3num_2g)

#Density plots of two groups along with the pooled plots
plot_2g <- plotdist(
  data_3num_2g,
  xmin = 10,
```

```
xmax = 125,  
title = "Example Density Plots of Two Groups",  
xlab = "x data",  
color.g1 = "skyblue",  
color.g2 = "pink",  
color.g1.pooled = "blue",  
color.g2.pooled = "red",  
label.g1 = "Treatment",  
label.g2 = "Control",  
display.legend = TRUE,  
pooled.dist = TRUE  
)  
print(plot_2g)
```

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